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Low Energy Neutron Measurements in High Energy Density Plasmas using the National Ignition Facility

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Deuterium-Tritium-loaded capsules at the National Ignition Facility (NIF) are now regularly producing a *neutron rich high energy density plasma* (nHEDP) with a low-energy "thermal" neutron density > 10^{21} neutrons/cm³. These low-energy neutrons are produced via multiple scatter off of the highly compressed capsule and therefore provide insight into the confinement time ($\tau_{confinement}$) of the assembled plasma. These neutrons are formed in the center of the 5 m NIF chamber, that is well suited to minimizing "room return" thermal capture. This nHEDP environment is well suited for activation-based measurements of the (n, γ) cross sections responsible for the formation of heavy elements in the interiors of massive stars. These experiments also offer the first opportunity to search for the effects of nuclear-plasma interaction-induced excited state population on (n,x) reaction rates in a stellar-like plasma environment. Unfortunately, no capability currently exists at the NIF to measure the neutron spectrum in a capsule down to the 100 eV level required to enable these new classes of nuclear-plasma experiments. In this paper we will discuss nHEDP-based neutron capture experiments, compare them to accelerator-based (n, γ) measurements, and discuss the requirements for a NIF-based low energy neutron spectrometer (LENS).

Keywords: ICF plasmas, neutron time-of-flight, nuclear-plasma interactions, stellar nucleosynthesis, s-process.

1. Introduction

The deuterium-tritium (DT) fuel in cryogenic capsules at the National Ignition Facility (NIF) is now regularly being assembled to areal densities (ρR_{fuel}) greater than any ever previously observed at an Inertial Confinement Fusion (ICF) facility [1]. While the primary goal of these experiments is to trap the α -particle energy from the D+T reaction in the dense fuel in order to achieve thermonuclear ignition, a "side effect" is that a significant fraction of the 14 MeV neutrons from the D+T reaction scatter until they "thermalize" to the keV energies of the assembled fuel. The number and spectral distribution of these thermal neutrons are an excellent probe of the temperature and plasma confinement time of the cold fuel, potentially providing

insight into the entropy of the cold fuel.

In addition to this role as a plasma diagnostic, these low-energy neutrons offer the first opportunity to study the neutron capture (e.g., (n,γ)) reactions responsible for the formation of the majority of the elements heavier than iron in the same sort of high energy density (HED) plasma environment in which they are formed in stars. This neutron-rich HED plasma (nHEDP) provides a laboratory capable of exploring the plasma-nuclear processes responsible for the population of excited nuclear levels in astrophysical settings [2]. While the potential for performing (n,γ) astrophysics measurements at ICF facilities has been recognized by the community [3], no neutron-capture capture products produced in the target assembly have ever been collected from an ICF-based experiment.

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However, starting in late 2011, the Solid Radchem Collector (SRC) [4] at NIF has been collecting radioactive ¹⁹⁸Au and ¹⁹⁶Au capture from (n,γ) and (n,2n) reactions on the ~100 mg of ¹⁹⁷Au in the NIF hohlraum using collectors that cover a modest ($\sim 10^{-4}$) portion of the total solid angle. The ratio of the ¹⁹⁸Au/¹⁹⁶Au reaction products collected by SRC is correlated with the down-scattered ratio of singly-scattered to un-scattered neutrons as determined using other neutron diagnostics. Model studies, confirmed by experiment, indicate that the dominant source of the 198 Au is due to the capture of scattered neutrons from the compressed capsule rather than lower energy (meV) "room return" neutrons which arise from scattering off of material the NIF chamber walls etc.. These results will be presented in greater detail elsewhere [5].

The SRC results open the door to NIF-based neutron activation cross section measurements utilizing mg-sized samples located on the NIF hohlraum. Plans are underway to perform "ride along" (n,y) experiments at the NIF in late 2013 using foils mounted on or near to the center of the NIF target chamber (TCC). measurements would complement existing methods of measuring (n,γ) using prompt γ -calorimetry and pulsed neutron beams [6]. However, these spectrally averaged (n,γ) cross section measurements require quantitative knowledge of the low-energy portion of the neutron spectrum. While time-of-flight (TOF) spectrometers are the tool of choice for measuring the neutron energy spectrum at NIF [7], their reliance on elastic scattering on hydrogen in the scintillator makes them insensitive to the low momentum imparted by sub-MeV neutrons. Efforts are therefore underway to design a highly segmented low-energy neutron spectrometer (LENS) for NIF. This system, which would be similar to the Large Neutron Scintillator Array (LANSA) spectrometer fielded at NOVA in the 1990s [8], will utilize novel boron and/or lithium loaded scintillators sensitive to low-energy neutrons coupled to modern state-of-the-art digital electronics and photomultiplier tube (PMT) technology.

The 198 Au SRC data provides not only the first evidence that neutron capture experiments can be performed at the NIF, but it also offers a potential platform for examining the effects of nuclear-plasma interactions in neutron-induced nuclear reactions for the first time. In addition to its long-lived ground state $J^{\pi}=2^{-}$ ground state (6.2 days), the 10.4 hour ¹⁹⁶Au metastable state is clearly evident in the NIF data. The 196mAu/196gAu ratio for Gold collected at the NIF could potentially be used to indicate density interaction of high level states populated 10⁻¹⁵ to 10⁻¹² s "quasi-continuum" following (n,2n) with the HEDP. This class of nuclear-plasma interactions has never been experimentally accessible before, and its existence would have dramatic consequences for our understanding of the formation of heavy nuclei in astrophysical settings.

2. Low-energy neutrons as a plasma diagnostic

Three conditions are needed to produce a significant low-energy neutron fraction in an ICF plasma:

- 1. A thermonuclear reaction neutron source (e.g., DT, DD, TT etc.)
- 2. A high fuel areal density (ρR_{fuel}) to allow scattering of the neutrons; and
- 3. A confinement time long enough to allow multiple scattering of neutrons in the cold fuel.

An indirectly driven cryogenic NIF hohlraum+capsule meets these criteria. These capsules, which start with an initial radius of approximately 1 mm, are compressed to a final radius on the order of 30-40 μ m. This compression causes the formation of peak DT areal densities in excess of 1 g/cm² capable of down-scattering primary 14 MeV

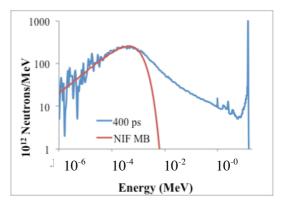


Fig.1 Hydrodynamic simulations of the neutron spectrum from a typical NIF DT shot (blue line) and a thermal distribution for kT=850 eV (red line).

neutrons to thermal energies. Furthermore, the modest yields achieved to date (Y_{total} < 2 kJ) allow for a primary neutron production in excess of several 10^{14} neutrons and a confinement time in excess of several 10^{-10} seconds.

Figure 1 above shows a typical neutron spectrum from advanced "post-shot" hydrodynamic simulations of a NIF shot. The inputs to these dynamic simulations are adjusted in order to reproduce the data from existing nuclear and x-ray diagnostics. The sub-keV portion of the neutron spectrum includes a broad peak that is well reproduced by a Maxwell-Boltzmann thermal distribution assuming kT=850 eV (blue line). Neutrons with energies below 850 eV have velocities of approximately 400 μ m/ns, allowing sufficient time for them to scatter multiple times in the 30 μ m cold fuel shell until they are "thermalized" with their local plasma environment. As the plasma expands ρR_{fuel} becomes too small to scatter

the neutrons effectively, thereby limiting the fraction of the neutrons in the "thermal peak" and making the thermal neutron fraction a confinement time (τ_{conf}) diagnostic.

Hydrodynamic simulations bear demonstrate this. Figure 2 below shows the neutron spectrum, including the low-energy component, for a simulation with conditions comparable to those believed to exist in NIF capsules for confinement times from 400-5000 ps. The fraction of neutrons below 1 keV differs by a factor of nearly 2.5 over this energy range.

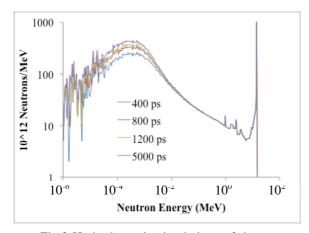


Fig.2 Hydrodynamic simulations of the neutron spectra from a NIF DT shot for τ_{conf} of 400, 800, 1200 and 5000 ps respectively.

3. Slow neutron capture nucleosynthesis

In addition to their value as a plasma diagnostic, (n,γ) reactions with keV neutrons are responsible for the formation of almost all of the elements heavier than iron made in astrophysical settings [2]. These reactions occur via both rapid neutron capture in very high-flux environments (the *r-process*) and slow neutron capture in massive stars throughout their lifetime (the *s-process*). The s-process environment exposes "seed" nuclei to neutron densities in excess of 10^{5-7}cm^{-3} in stellar plasmas with temperatures from 0.1-1.0 billion degrees Kelvin ($kT \approx 8-86 \text{ keV}$). These capture processes take place at a rate defined by the neutron capture cross sections $(\sigma_{m,j} \approx 10^{-24} \text{ cm}^2)$, and the neutron velocity (v_n) :

$$R_{(n,\gamma)} = \rho_n v_n \sigma_{(n,\gamma)} = 0.1 / year$$
 [1]

Neutron capture proceeds along a chain of isotopes for a given element until a radioactive nucleus is formed whose lifetime is comparable to or shorter than the capture rate. If the lifetime is significantly shorter, β -decay will occur.

However, if the lifetime of the radioactive product is comparable to the capture rate, a branching takes place where β -decay and neutron capture compete. Figure 3 shows an example of the s-process pathway along near

barium and cesium, including the branch point at the nucleus 134 Cs ($t_{1/2}$ =46 days) from [2].

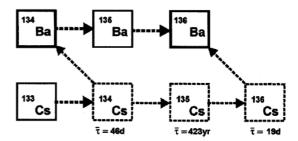


Fig 3: s-process pathway near cesium (Z=55) and barium (Z=56) reproduced from *Busso*. Note that branching occurs on nuclei where the lifetime is comparable to the inverse capture rate (≈ 0.1 -1 year⁻¹).

Capture on "branch-point" nuclei offers a unique window into the conditions in the interior of massive stars and plays a critical role in the development of stellar models. However, its usefulness is limited by a lack of knowledge of the neutron capture cross section on these radioactive branch point nuclei themselves. This need has been identified by the community [9] and has led to a significant effort to determine these cross sections at astrophysically relevant energies.

Unfortunately, (n,y) cross sections are difficult to model accurately. This sensitivity has been most recently demonstrated by Kappeler's group at Karlsruhe [10], which has been measuring Maxwellian-Averaged Cross Sections (MACS) corresponding to thermal neutron energy distributions at s-process temperatures (e.g., 4-25 keV) for more than two decades. The Karlsruhe group informed six leading members of the nuclear reaction modeling community of their intention to measure neutron MACS for two hafnium isotopes, ¹⁷⁴Hf and ¹⁸²Hf. Modelers were asked to predict the values for the MACS for these two nuclei prior to their measurement. Figure 4 below shows the results of these predictions, which span a factor of 3 for ¹⁷⁴Hf and a factor of 6 for ¹⁸²Hf, together with the value measured by the Karlsruhe group. These differences highlight the uncertainties in keV neutron capture modeling and significantly impair s-process modeling efforts.

An additional complication exists with regard to (n,γ) in HEDP environments. Neutron capture rates are highly sensitive to small changes in the spin of the target nucleus. However, while nuclei are generally in their ground state in non-plasma environments, a significant portion of them have low-lying states with different spins that can be thermally populated in a nHEDP. The interactions that populate these states, including nuclear

excitation by electron capture (NEEC) and nuclear excitation by electronic transition (NEET) have been the subject of extensive work [11,12] and are the subject of

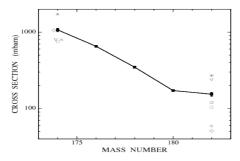


Fig 4: Modeled (open symbols) and predicted values for neutron capture MACS on ¹⁷⁴Hf and ¹⁸²Hf together with those measured by the Karlsruhe group (closed circles).

an intense research effort in their own right. The alteration of the (n,γ) cross sections arising from the change in spin due to excited state population is parameterized in s-process models via a *stellar* enhancement factor (SEF) that can range from 0.8-1.4 times the (n,γ) cross section on the ground state.

4. Neutron capture at ICF and accelerator facilities

Neutron capture is unlike charged particle induced nuclear reactions in that the lack of a Coulomb barrier causes (n,x) reaction cross sections to increase with the increasing deBroglie wavelength (decreasing energy) of the neutron. This feature makes activation-based keV (n,γ) cross sections measurements inherently difficult to perform since even a small number of lower-energy "room return" neutrons will have a significantly higher probability to induce activation in the target.

In addition to the issue of room return, many astrophysically-relevant (n,γ) cross sections involve radioactive targets with half lives on the order of hundreds of days, leading to huge y-ray decay rates for targets handled in a laboratory. For example, a one mg sample of the ¹³⁴Cs branch point nucleus has a decay rate of 1 curie. As a result, efforts to measure (n, γ) on radioactive nuclei have focused high-segmentation arrays to observe the relatively high total γ-ray energy (~6-9 MeV) signal released following capture over the background of energy released due to radioactive decay of the target. The Device for Advanced Neutron Capture Experiments (DANCE) spectrometer at Los Alamos is a good example of a calorimetric system [6] designed to perform (n,y) cross section measurements on radioactive targets. DANCE spectrometer is an array of 160 highly segmented BaF detectors at the Los Alamos Neutron

Science (LANSCE). LANSCE provides a "white" neutron source with a flux of $\approx 10^4$ n/s/cm²/keV where the neutron energy is determined via time-of-flight (TOF). The array is located twenty meters away from the neutron source, meaning that only a small fraction of the neutron beam interacts with the target. While DANCE has produced a wealth of nuclear structure information on stable targets, it has yet to measure an astrophysically relevant (n,γ) cross section on an *s*-process branch point nucleus with a hard γ -ray decay component.

An ICF-driven neutron source provides an alternative approach to measuring keV neutron-capture cross sections using activation. Nuclei in the inner layer of a NIF capsule are subject to a neutron fluence greater than 10¹⁵ n/cm²/keV and a flux of nearly 10²⁵ n/cm²/keV/s. Furthermore, these target nuclides are located in the middle of the NIF chamber, which is essentially a 5 m radius empty sphere surrounded by a thick sleeve of borated concrete material known as "gunnite". placement is ideal for minimizing background neutrons from local scattering and "room return" neutrons. However, instead of lower-energy background neutrons, a neutron capture sample in NIF experiences a large fluence of 14 MeV primary neutrons. These neutrons, while sizable in number, have significantly lower capture cross sections compared to keV neutrons. Furthermore, the contribution of 14 MeV neutrons to capture can be quantified using a NIF capsule referred to as an "exploding pusher" designed to produce few, if any, low energy neutrons.

While NIF as a neutron source compares favorably with existing facilities like LANSCE, as well as proposed future facilities, such as FRANZ [10], a number of issues need to be addressed before an ICF-based (n,γ) measurement can take place. Foremost amongst these is the lack of a well-characterized neutron spectral diagnostic for the low-energy neutrons that dominate the capture process.

5. Characteristics of a Low-Energy Neutron Spectrometer for ICF (n,γ) measurements

A Low Energy Neutron Spectrometer (LENS) capable of measuring the low-energy neutron spectrum at an ICF facility would require several features including:

- 1. High segmentation to increase data bandwidth in a given time interval
- Location at sufficient distance from TCC to allow for good energy resolution using time-of-flight (most likely at a 20 m TOF positions)
- 3. The use of neutron detectors inherently sensitive to low-energy neutrons

4. Digital electronic readout to maximize the information contained in the detector trace and to allow "seamless" transition from current mode (where individual neutron hits are not resolved) to pulse mode (where individual hits are resolved and pulse-height thresholds can be employed)

The LANSA spectrometer fielded at the Nova laser [8] satisfied these requirements. LANSA was comprised of 960 individual scintillator channels and fielded 20 m from the Nova target. The spectrometer was used to measure primary neutrons directly arising from thermonuclear reactions for ICF shots with yields as low as several 10^5 neutrons and operated solely in pulse mode. A NIF-based LENS capable of resolving individual neutron hits in a similar fashion for a 10^{14} neutron NIF shot would require an impractically large number of channels. Instead, a NIF-based system would measure the energy of incoming neutrons in current mode for neutrons with energies greater than a critical energy E_{crit} given by:

$$\varepsilon_{\text{det}}(E_{crit}) \times d\Omega_{\text{det}} \times \phi_n(E_{crit}) \times \Delta t_{crit} \ll 1$$
 [2]

Here ε_{det} is the efficiency, $d\Omega_{det}$ is the areal coverage, and Δt_{det} is the time response of a given LENS detector element and ϕ_n is the neutron flux at the location of the spectrometer. LENS would then "cross-over" to individual pulse mode for neutron energies below E_{crit} functioning in a similar manner to LANSA. For energies below E_{crit} LENS could be absolutely calibrated using a non-ICF neutron source with a well-defined neutron flux. A LENS would be calibrated and function in a manner similar to the existing NIF NTOF system for energies above E_{crit} . Early results using the new NIF NTOF system near the "south pole" of the target chamber are consistent with this current to pulse mode transition occurring for t > 4 μ s.

Consider for example a 256-element LENS array located 20 m from TCC at NIF that is tasked with observing the late-time (low energy) neutron spectrum. Figure 5 below shows the relative number of neutrons observed in such a LENS as a function of TOF for the modeled NIF DT shots with values of τ_{conf} shown in Figure 3 above. The ratios differ by nearly 50% for a neutron TOF of 100 μ s, corresponding to $E_n \approx 200$ eV.

Fast organic crystal scintillators have been used quite successfully in current mode at NIF for the detection of neutrons with energies > 140 keV [14]. However, these scintillators are not well suited to the task of detecting low-energy neutrons due to their reliance on elastic scattering of hydrogen to convert the neutron

kinetic energy to light. This issue can be rectified through the addition of a dopant that leads to the production of charged particles with a large, positive Q-value and cross section at low E_n . Two frequently employed dopants are lithium and boron. These nuclei are highly sensitive to low energy neutrons through the ${}^6\text{Li}(n,t)\alpha$ and the various ${}^{10.11}\text{B}(n,x)2\alpha$ reactions.

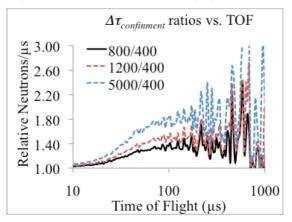


Fig.5 Hydrodynamic simulations showing the ratio of the number of neutrons/ μ s arriving 20 m from TCC following a NIF DT shot for τ_{conf} of 800 ps (black), 1200 ps (red) and 5 ns (blue) relative to τ_{conf} = 400 ps. Note that 100 μ s corresponds to a neutron energy of \approx 200 eV

Furthermore, Li-doped glass has been employed at the GEKKO laser facility [15], and boron-loaded scintillators, such as BC-454 from Saint-Gobain are commercially available.

6. LENS testing at the LBNL 88-Inch cyclotron

The LENS prototype system and its various candidate scintillator materials can be tested and calibrated using a variety of accelerator-based neutron sources. One such facility is the thick-target deuteron break-up neutron source at the LBNL 88-Inch Cyclotron. This facility was used in the study and testing of the new bibenzyl-based scintillator developed for NIF [14]. Figure 6 shows a schematic of the neutron beam line at the cyclotron. Deuterons beams with currents up to ten µA are made incident upon a thick target where up to 10% of the beam is fragmented into its constituent protons and neutrons. The protons and unreacted deuterons stop in a thick water-cooled target, while the neutrons travel through approximately 2 m of concrete collimation plus an additional two to eight meters of air before entering the experimental area. The cyclotron beam consists of individual pulses with a width ≥ 1 ns and a pulse spacing on the order of 100 ns allowing their energy to be determined using TOF. The resulting neutron energy spectrum is broad (typically several MeV), but centered

slightly below half of the beam energy and is well described in the literature [16,17]. Recent activation measurements have confirmed the published neutron spectrum, and the first testing of candidate scintillator materials for LENS is underway.

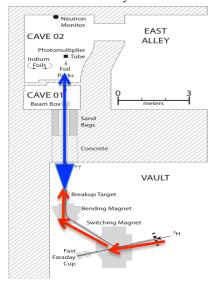


Fig.6 Layout of the neutron source at the 88-Inch cyclotron. Deuterons (**red arrows**) incident on a break-up target in the cyclotron vault form a neutron beam (**blue cone**) collimated in the shielding wall prior to hitting the scintillator (**star**).

6. Conclusion

ICF facilities present a unique environment for studying neutron capture in plasma environments due to the presence of a significant low-energy neutron component arising from the multiple scatter of neutron on the highly compressed hydrogen fuel. These low-energy neutrons offer a direct measurement of the confinement time of the assembled plasma and open the possibility of astrophysically relevant (n,y) cross section measurements. However, all of these ICF-based neutron studies require a quantitative understanding of the low-energy neutron spectrum. An effort is underway to develop an appropriate low-energy neutron spectrometer for use at NIF following the approach pioneered at NOVA by Nelson and Cable [8] using the intense neutron source at the LBNL 88-Inch Cyclotron.

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